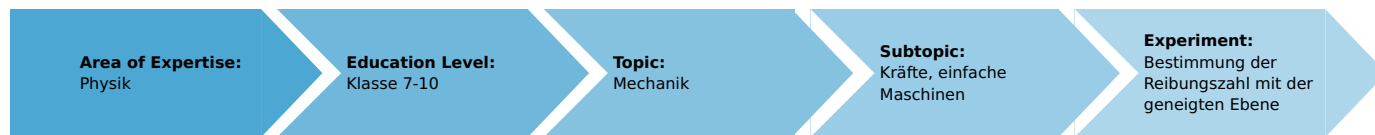


# Determination of the coefficient of friction on an inclined plane (Item No.: P1253000)

## Curricular Relevance



### Difficulty



Intermediate

### Preparation Time



10 Minutes

### Execution Time



20 Minutes

### Recommended Group Size



1 Student

**Additional Requirements:**

**Experiment Variations:**

**Keywords:**

## Principle and equipment

### Principle

Demonstrate that one can determine the coefficient of friction  $\mu$  on an inclined plane without measuring any forces.

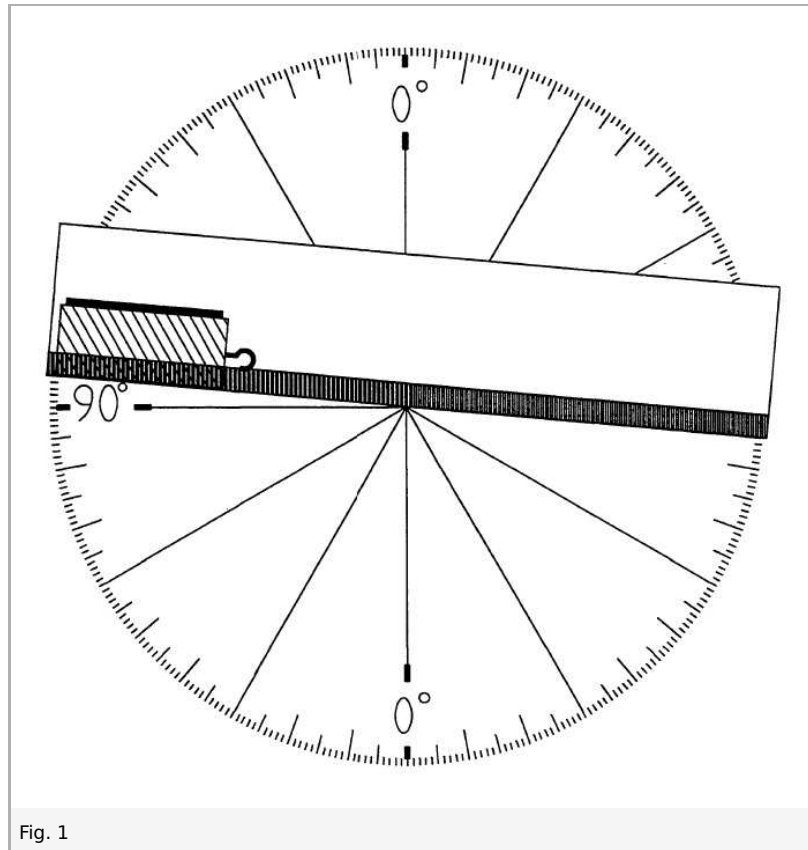
### Equipment

Position No.	Material	Order No.	Quantity
1	Demo Physics board with stand	02150-00	1
2	Inclined plane f.demonstr.board	02152-00	1
3	Optical disk, magnet held	08270-09	1
4	Friction block	02240-01	1
5	Scale for demonstration board	02153-00	1
6	Holding pin	03949-00	1
7	Slotted weight, black, 50 g	02206-01	2

## Set-up and procedure

### Set-up

- Place the protractor disk onto the demonstration board.
- Attach the plane on the protractor disk in such a manner that its lower edge passes through the centre of the protractor disk.
- Beginning with a slight angle of inclination  $\alpha$  between the plane and the horizontal line on the protractor disk, place the friction block onto the inclined plane with its larger wooden surface downwards (Fig. 1).



### Procedure

- Increase the size of the angle of slope  $\alpha$  gradually, in such a manner that the plane rotates around the centre of the protractor disk.
- Read the angle  $\alpha_h$  which is required so that the contact frictional force  $\vec{F}_h$  is just overcome and the block begins to slide; read  $\alpha_h$ .
- Without changing the angle  $\alpha_h$  place the block onto the inclined plane several times and carefully observe its movement.
- Record  $\alpha_h$  and your observations (1).
- Return the inclined plane to its initial position, increase the angle of slope  $\alpha$  as before, but now before the angle  $\alpha_h$  is reached, determine the angle  $\alpha$  at which the friction block slides down the inclined plane after being pushed lightly by trial and error; observe the block carefully; note the value of  $\alpha$  (in Table 1) and your observation (2).
- With the aid of the holding pin, first load the friction block with one of the slotted weights, then with both of them. Determine the angle  $\alpha$  in each case and record it.

## Observations and evaluation

### Observations

1. After overcoming the contact frictional force, the block slides increasingly rapidly down the inclined plane.
2. Table 1

Friction block	Table 1	$\alpha/1^\circ$
Without load		10
Loaded with 50 g		10
Loaded with 100 g		10

The block slides - whether unloaded or loaded - down the slope with uniform movement after being pushed lightly.

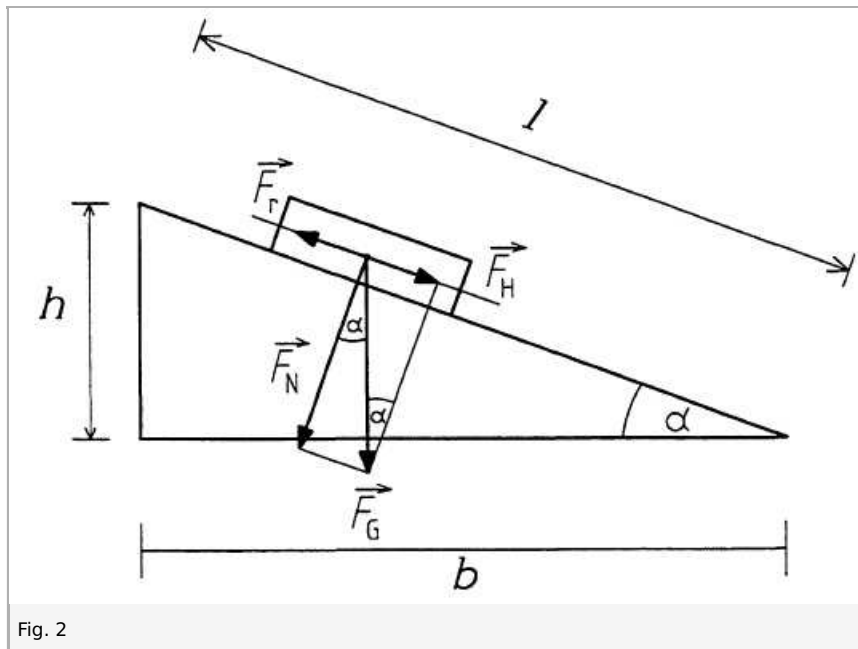
### Evaluation

The following is true for the inclined plane:

$$F_H = \frac{F_G \cdot h}{l} = F_G \cdot \sin \alpha \text{ (cf. Fig. 2)}$$

If a body slides down the inclined plane uniformly (with constant velocity), the movement against the opposing frictional force  $\vec{F}_r$ , which equal to the downslope driving force  $\vec{F}_H$  in magnitude. Therefore, the following is valid:

$$\vec{F}_H = \vec{F}_r = F_G \cdot \sin \alpha .$$



In addition, the following is true for the (sliding) frictional force:

$$\vec{F}_r = \mu \cdot \vec{F}_N$$

where  $\vec{F}_N$  indicates the normal force, which acts perpendicular to the inclined plane as a component of the weight  $\vec{F}_G$ .

Consequently,  $F_G \cdot \sin \alpha = \mu \cdot F_G \cdot \cos \alpha$  (cf. Fig. 2). From this it follows that  $\mu = \tan \alpha$ , a result which generally surprises the student because, according to it,  $\mu$  is not a function of the normal force.

With the equation  $\mu = \tan \alpha$ , an easily applied measuring equation for the determination of the coefficient of friction is available. The last part of the experiment, which should only serve to confirm the equation  $\mu = \tan \alpha$ , establishes that  $\mu$  is

independent of the weight  $\vec{F}_G$  and thus of the normal force  $\vec{F}_N$ .

The results of the first part of the experiment show that the static frictional force is larger than the sliding frictional force since  $F_H > F_r$ . And because the downslope driving force is larger in this case than that required to compensate the sliding frictional force, the movement is accelerated.

### Remarks

If the students do not have any previous trigonometric knowledge, then  $h$  and  $b$  can be measured and as a result of  $\frac{F_H}{F_G} = \frac{h}{b}$  (cf. Fig. 2), the relationship  $\mu = \frac{h}{b}$  instead of  $\mu = \tan \alpha$  can be used to determine  $\mu$ . Logically, this changes nothing in the recognition that  $\mu$  is independent of  $F_N$ .

While turning the inclined plane, one must avoid jerky changes. Otherwise, the determination of the angle  $\alpha_h$  and  $\alpha$  becomes more difficult. If one changes the position of the plane progressively (each step  $1^\circ$ ) in the vicinity of  $\alpha_h$  and  $\alpha$ , and in each case replaces the frictional block, the experimental procedure is usually facilitated.

If one desires to have larger angles  $\alpha_h$  and  $\alpha$ , the block must be placed with its rubberised side downwards.

